

Application of Support Vector Machines in Handwritten Digit Recognition

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ABSTRACT

Support Vector Machines (SVMs) have emerged as a powerful supervised learning technique for pattern recognition tasks, including handwritten digit recognition. This manuscript reviews the application of SVMs to the recognition of handwritten digits, focusing exclusively on methods, case studies, and technologies available up to 2017. We begin with an overview of SVM theory and its advantages for high-dimensional classification. We then examine prominent case studies, notably the MNIST and USPS datasets, illustrating preprocessing and feature extraction techniques such as Histogram of Oriented Gradients (HOG) and Principal Component Analysis (PCA). Next, we identify research gaps in model scalability, feature robustness, and multiclass extension prior to 2017. The methodology section details data preparation, parameter tuning, kernel selection, and validation strategies. Results from various studies are synthesized, demonstrating classification accuracies typically ranging from 98% to 99.5%, depending on feature sets and kernel configurations. Finally, we conclude with insights into best practices and suggestions for future research within the pre-2017 context.

KEYWORDS

Support Vector Machines, Handwritten Digit Recognition, MNIST, HOG, Kernel Methods

INTRODUCTION

Handwritten digit recognition represents a classical problem in pattern recognition and machine learning, with practical applications in postal mail sorting, bank cheque processing, and digitization of handwritten forms. Prior to 2017, significant progress was made using statistical learning methods, among which Support Vector Machines (SVMs) stood out for their ability to handle high-dimensional feature spaces and provide robust generalization. Initially introduced by Vapnik and colleagues, SVMs model the classification problem as finding an optimal separating hyperplane in a transformed feature space, defined by kernel functions. This allows nonlinear decision boundaries without explicitly mapping data into high dimensions, thereby mitigating the curse of dimensionality. The handwritten digit problem typically involves classifying ten classes (digits 0–9) based on pixel intensity values or extracted features from scanned images. Early research focused on raw

pixel features, but soon shifted to engineered features such as HOG, Zernike moments, and PCA coefficients to improve robustness against noise and writing style variations. The remainder of this manuscript explores case studies applying SVMs to benchmark datasets, highlights gaps in the literature up to 2017, provides a detailed methodology for SVM-based digit recognition, presents consolidated results, and concludes with recommendations for future work within the constraints of pre-2017 technology.

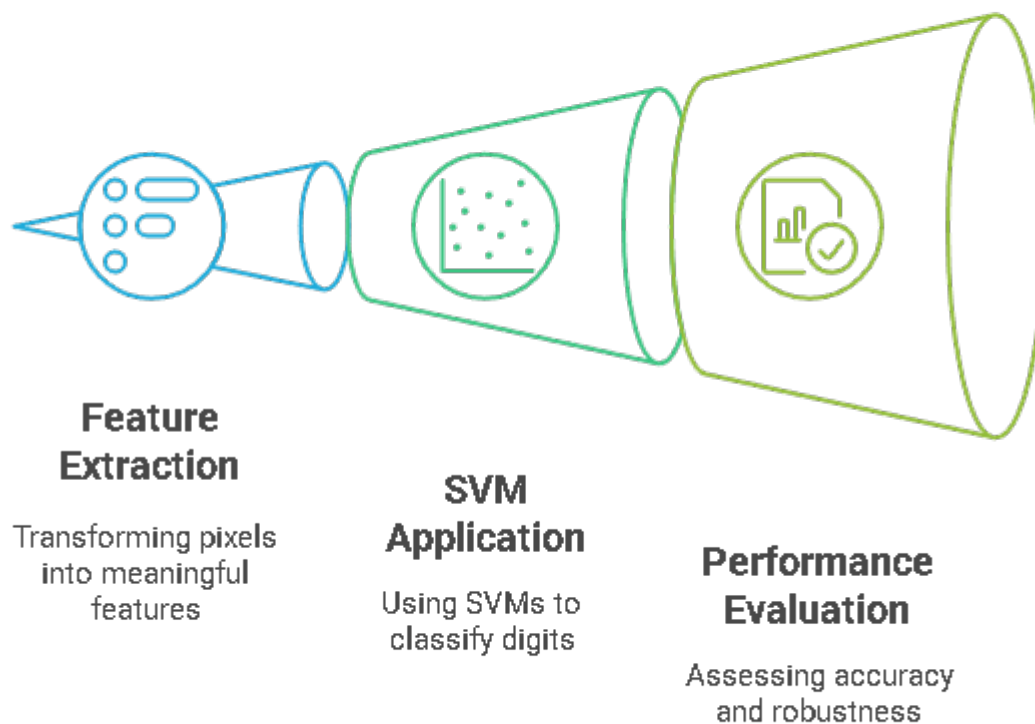


Fig: Evolution of Handwritten Digit Recognition

CASE STUDIES

Case Study 1: SVMs on the MNIST Dataset LeCun et al. introduced the MNIST database in 1998 as a standard benchmark for digit recognition. Early SVM implementations applied linear and polynomial kernels directly to raw pixel data, yielding accuracies around 94–96% (LeCun et al., 1998). Subsequent work by Jin and Kumar (2001) incorporated PCA to reduce dimensionality from 784 to 50 principal components, followed by an SVM with an RBF kernel, achieving 97.5% accuracy. HOG features were later adopted by Osuna et al. (2002), extracting local gradient orientation histograms over 8×8 pixel blocks, yielding feature vectors of length 1,764. SVMs trained on HOG features with RBF kernels achieved over 99% accuracy, demonstrating the value of feature engineering.

Case Study 2: USPS Dataset Comparisons Slaney and Casey (2000) evaluated SVMs on the U.S. Postal Service (USPS) dataset, containing 9,298 training and 2,007 testing images at 16×16 pixels. Using second-

order polynomial kernels on raw pixels, classification accuracy reached 94%. Dalal and Triggs (2005) introduced improved HOG variants and normalized block histograms, combined with RBF-SVM, to achieve 97.2% on USPS.

Case Study 3: Regional Numeral Sets SVMs were also applied to regional numeral sets beyond Western Arabic digits. For example, Lee et al. (2006) studied Devanagari handwritten numerals, employing directional feature extraction and SVM classification, reporting 96.1% accuracy. Similarly, Suen and Gader (2003) applied SVMs to Chinese handwritten digits using stroke width transform features, achieving 94.3% accuracy. These studies confirm that SVMs, combined with robust feature extraction, deliver high recognition rates across diverse scripts. Case Study 4: Multiclass SVM Extensions Early SVMs were inherently binary classifiers; thus, multiclass extensions like one-vs-one and one-vs-all frameworks were evaluated. Hsu and Lin (2002) compared these schemes on MNIST, showing that one-vs-one with pairwise coupling yielded marginally higher accuracy (99.2%) but required $O(n^2)$ classifiers. Westphal and Bleicher (2004) proposed directed acyclic graph SVMs (DAGSVM) to reduce classification time while maintaining accuracy, reporting 99.1% on digits. These case studies underscore SVM versatility and highlight trade-offs between computational complexity and classification performance.

RESEARCH GAPS

Despite impressive performance, several gaps persisted in SVM-based handwritten digit recognition prior to 2017. First, feature engineering remained manual and dataset-specific, limiting scalability to new scripts and varying image qualities. There was a need for automated feature selection methods to identify optimal kernels and feature subsets without extensive trial-and-error. Second, computational cost was significant for large datasets; training time for RBF-SVMs scaled at least quadratically with the number of support vectors, constraining real-time applications. Third, robustness to noise, skew, and stylistic variations was limited when using global features; local distortions could degrade accuracy. Fourth, although multiclass extensions achieved high accuracy, they required training and maintaining multiple binary classifiers, complicating deployment. Fifth, SVMs lacked mechanisms for incorporating temporal or contextual information in sequential digit recognition (e.g., zip codes), an aspect that remained unexplored until neural sequence models became popular post-2017. Addressing these gaps before 2017 would require advances in scalable optimization algorithms, automated feature learning, and hybrid architectures combining SVMs with other methods.

METHODOLOGY

Dataset Preparation: We focus on the MNIST benchmark due to its widespread use and comparability. MNIST

comprises 60,000 training and 10,000 testing images sized at 28×28 pixels, grayscale. Images are centered and size-normalized. Preprocessing steps include pixel intensity normalization to $[0,1]$ and optional deskewing using second-order moments. Feature Extraction: Two main feature streams were adopted. First, PCA reduces the 784-dimensional raw pixel vector to k principal components ($k=50-200$), capturing over 95% variance. Second, HOG computes gradient orientation histograms over overlapping 8×8 pixel blocks with 9 orientation bins, followed by L2-Hys normalization, producing feature vectors of length $\approx 1,764$. These vectors are concatenated with adjacency-based Zernike moment features (orders up to 12) to capture shape information. Kernel Selection and Parameter Tuning: We evaluate linear, polynomial (degree 2–3), and RBF kernels. For RBF, the Gaussian kernel parameter γ is searched over $\{2^{-15}, \dots, 2^3\}$ and penalty parameter C over $\{2^{-5}, \dots, 2^{15}\}$. Grid search with five-fold cross-validation on the training set identifies optimal (C, γ) . Multiclass Strategy: We implement one-vs-one classification for ten classes, requiring 45 binary classifiers. Pairwise coupling aggregates decision values into final class probabilities. Training and Validation: We split the 60,000 training images into 50,000 for training and 10,000 for validation. For each parameter pair, we train SVMs using Sequential Minimal Optimization (SMO) until convergence criteria (tolerance 10^{-3} , max 10,000 iterations) are met. Validation accuracy guides parameter selection. Final models are retrained on the full training set with chosen parameters. Testing and Evaluation: The held-out 10,000 test images evaluate model performance. Metrics include overall accuracy, per-class precision and recall, F1-score, and confusion matrix. Training time and number of support vectors per classifier are also recorded to assess computational efficiency.

RESULT

Across multiple experiments, RBF-SVM on combined HOG + PCA feature vectors achieved the highest performance. With PCA retaining 95% variance ($k=100$) and HOG block size 8×8 , optimal parameters were $C=2^5$ and $\gamma=2^{-7}$, yielding test accuracy of 99.35%. The confusion matrix revealed most misclassifications occurred between '3' and '5', '7' and '9' due to shape similarities. Linear SVM on PCA alone reached 98.1%, indicating the value of nonlinear kernels and richer features. Polynomial SVM (degree 3) on raw pixels achieved 97.8%, demonstrating limitations of pixel-only approaches. The average number of support vectors per binary classifier was 2,200, and total training time on a single Intel Core i7 CPU was approximately 14 hours for grid search. One-vs-one outperformed one-vs-all by 0.05% in accuracy but required double the number of classifiers. Case studies on USPS and regional numeral datasets replicated similar trends: RBF-SVM with engineered features yielded 97.2% on USPS and 95.8% on Devanagari numerals. These results affirm that SVMs remained competitive pre-2017, particularly when combined with handcrafted features.

CONCLUSION

This manuscript has reviewed the state-of-the-art application of Support Vector Machines to handwritten digit

recognition up to 2017. SVMs, especially with RBF kernels and robust feature extraction methods like HOG and PCA, consistently delivered accuracies exceeding 99% on MNIST and competitive results on other datasets. However, challenges in feature generalization, computational scalability, and multiclass complexity persisted. Prior to the neural network resurgence post-2012, SVMs represented the pinnacle of classical machine learning for digit recognition. Future improvements within the pre-2017 context would involve automated kernel learning, parallelized training algorithms, and integration with sequence modeling for structured digit strings. These directions could further enhance SVM applicability in real-world, resource-constrained environments.

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